

Chapter 8: Systems of Equations

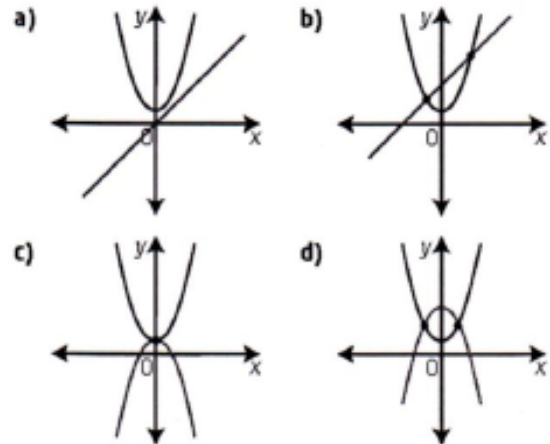
1. Examine each system of equations and **match it** with a possible sketch of the system. You do not need to solve the systems to match them.

I) $y = x^2 + 1$
 $y = -x^2 + 1$ c

II) $y = x^2 + 1$
 $y = x$ a

III) $y = x^2 + 1$
 $y = -x^2 + 4$ d

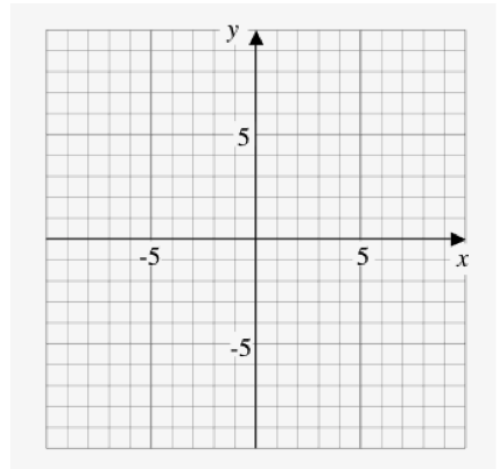
IV) $y = x^2 + 1$
 $y = x + 4$ b



2. Solve the system of linear-quadratic equations graphically. Express your answer(s) to the nearest tenth.

$$3x + y = 4$$

$$y = x^2 - 3x - 1$$



(2.2,-2.7) and (-2.2,10.7)

3. Given the quadratic function $y = x^2 + 4$ and the linear function $y = x + b$, determine all the possible values of b that would result in a system of equations with:

- a) two solutions
- b) exactly one solution
- c) no solution

- a) $b > 4$ b) $b = 4$ c) $b < 4$

4. The price, P , in dollars, per share, of a high-tech stock has fluctuated over a 10-year period according to the equation $P = 14 + 12t - t^2$, where t is time, in years. The price of a second high-tech stock has shown a steady increase during the same time period according to the relationship $P = 2t + 30$. Algebraically determine for what values the two stock prices will be the same.

\$34 and \$46

5. Explain how you could determine if the given system of quadratic-quadratic equations has zero, one, two, or an infinite number of solutions without solving or using technology.

$$y = (x - 4)^2 + 2$$

$$y = -(x + 3)^2 - 1$$

Compare vertices and opening directions. Never cross -> no solution.

6. Algebraically determine the solution(s) to each system of quadratic-quadratic equations.

a) $y = 2x^2 + 9x - 5$
 $y = 2x^2 - 4x + 8$

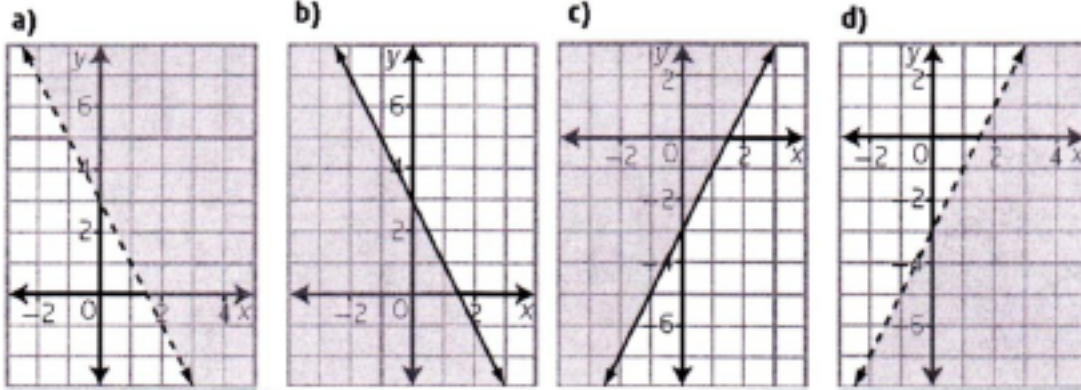
b) $y = 12x^2 + 17x - 5$
 $y = -x^2 + 30x - 5$

(1,6)

(0,-5) and (1,24)

Chapter 9: Linear & Quadratic Inequalities

7. Match each inequality with its graph.



I) $2x + y < 3$ ___a___

II) $2x - y \leq 3$ ___c___

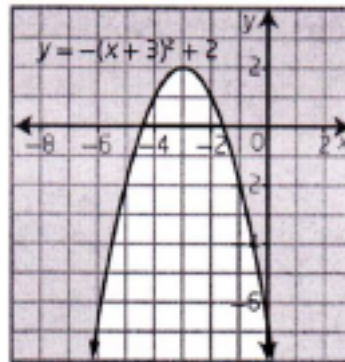
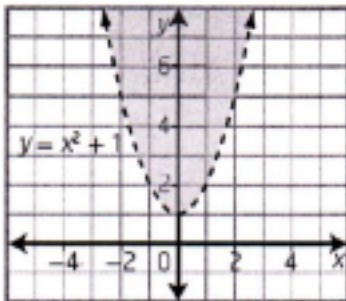
III) $2x - y \geq 3$ ___b___

IV) $2x + y > 3$ ___d___

8. Write an inequality to describe each graph, given the function defining the boundary parabola.

a) $y > x^2 + 1$

b) $y \geq -(x+3)^2 + 2$



9. Explain how each test point can be used to determine the solution region that satisfies the inequality $y > x - 2$

Plug in

a) (0, 0)

b) (2, -5)

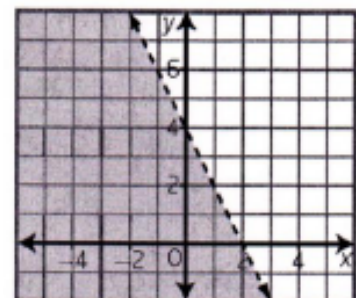
c) (-1, 1)

yes

no

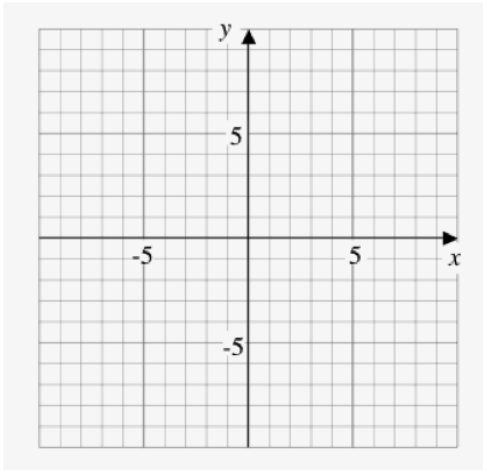
yes

10. What linear inequality is shown in the graph?



$y < -2x + 4$

11. Sketch the graph of $y < x^2 - 6x + 5$. Use a test point to verify the solution region.



dotted, shade below (use graph calc if desired)

12. Use sign analysis to determine the solution of the quadratic inequality $2x^2 + 9x - 37 \geq 2$.

$$x \leq \frac{-9 - \sqrt{393}}{4} \text{ and } x \geq \frac{-9 + \sqrt{393}}{4}$$

13. Suppose a rectangular area of land is to be enclosed by 1000 m of fence. If the area is to be greater than $60\,000 \text{ m}^2$, what is the range of possible widths of the rectangle?

Width is in between 200 m and 300 m